

1. If  $f(x) = 4x^3 + 7$ , does  $f^{-1}$  exist? If so, find it. If not, explain why not.
2. Simplify  $\tan(\cos^{-1}(\frac{3}{x}))$ .
3. Simplify  $\csc(\sin^{-1}(\frac{3}{x}))$ .
4. Determine whether the function is one to one.
  - (a)  $f(x) = 2x + 4$ .
  - (b)  $f(x) = |x|$ .
  - (c)  $f(x) = x^2 - 2x$ .
5. Find the inverse of function of  $f$ .
  - (a)  $f(x) = 3x + 5$ .
  - (b)  $f(x) = \frac{2-x^3}{5}$ .
6. Find the domain and range of  $f(x) = \sqrt{9 - x^2}$ .
7. Determine whether  $f(x) = 2x^5 - 3x^2 + 2$  is odd, even or neither.
8. Find the functions  $f \circ g$ ,  $g \circ f$ ,  $f \circ f$  and  $g \circ g$  where  $f(x) = 3x - 1$  and  $g(x) = 2x - x^2$ .
9. Simplify  $\sin(\sin^{-1} \frac{1}{4})$ .
10. Simplify  $\cos^{-1}(\cos \frac{5\pi}{6})$ .
11. Simplify  $\tan(\sin^{-1} \frac{1}{2})$ .
12. If for a function  $f(x)$ ,  $f(x + y) = f(x) + f(y)$  for all reals  $x$  and  $y$  then  $f(0)$  is equal to
  - (a) 1
  - (b) 0
  - (c)  $f(x) \forall x \in \mathbb{R}$
  - (d) None of these

13. If  $x$  be real then the range of the function  $f(x) = \frac{x}{1+x^2}$  is

- (a)  $[-1/2, 1/2]$
- (b)  $(-2, 2)$
- (c)  $(-1, 1)$
- (d)  $(-1/2, 1/2)$

14. If  $f(x) = \frac{1}{1-x}$ ,  $g(x) = f(f(x))$  and  $h(x) = f(f(f(x)))$ , then  $f(x) \cdot g(x) \cdot h(x)$  is equal to

- (a)  $\frac{1}{(1-x)^3}$
- (b)  $\frac{1}{1-x}$
- (c) 1
- (d) -1